

Home assignments for the Course of Polymer Physical Chemistry

Third section of the course: Polymer Conformations

1. Calculate the mean unperturbed radius of gyration R_g for poly(methyl methacrylate) with molecular weight 100,000; and for polyisoprene with molecular weight 6,800.

$$R_g = \sqrt{\frac{2 \frac{M}{m_o} C_\infty l^2}{6}} = 0.154 nm \sqrt{\frac{1000 * 9}{3}} \approx 8.4 nm \quad \text{for PMMA}$$

$$R_g = \sqrt{\frac{4 \frac{M}{m_o} C_\infty l^2}{6}} = 0.154 nm \sqrt{\frac{2 * 100 * 4.6}{3}} \approx 2.7 nm \quad \text{for PI}$$

2. Calculate the mean radius of gyration for DNA molecule with 1 million base pairs. Assume that the distance between base-pairs is 0.33 nm, and the persistence length is 50 nm.

$$R_g = \sqrt{\frac{2aR_{\max} \left[1 - \frac{a}{R_{\max}} \left\{ 1 - \exp\left(-\frac{R_{\max}}{a}\right) \right\} \right]}{6}} \approx \sqrt{\frac{50 * 330,000}{3}} nm \approx 2.35 \mu m$$

3. Assume a chain with 1000 segments, each has length 2 nm. Calculate how much larger will be the mean end-to-end distance of this chain in good solvent relative to its end-to-end distance in Θ -solvent.

$$R_n(\theta) = b\sqrt{N} \approx 63 nm;$$

$R_n(\text{good}) \approx bN^{3/5} \approx 126 nm$; The end-to-end distance of the given molecule in good solvent is ~ 2 times larger than in Θ -solvent. The same can be obtain in easier way:

$$\frac{R_n(\text{good})}{R_n(\theta)} \approx \sqrt{N^{1/5}} \approx 2$$