

Home assignments for the Course of Polymer Physical Chemistry

Fourth section of the course: Polymer Solution and Blends

1. Polymer with N segments is in a solution. The polymer-solvent interaction parameter $\chi=100K/T$. How the temperature range of miscibility changes with the length of the chain?

$$T_C = \frac{B}{\frac{1}{2}\left(1+\frac{1}{\sqrt{N}}\right)^2} = \frac{200}{\left(1+\frac{1}{\sqrt{N}}\right)^2}K$$

This is the case of Upper Critical Solution Temperature because the c parameter decreases with temperature increase. The miscibility temperature range $T > T_C$. T_C increases from 50K for $N=1$ up to 200K at $N \rightarrow \infty$.

2. Polymer with $N=100$ segments in a solution has the polymer-solvent interaction parameter $\chi=-50K/T+0.8$. Define the temperature range of miscibility of the polymer in the solvent.

$$T_C = \frac{B}{\frac{1}{2}\left(1+\frac{1}{\sqrt{N}}\right)^2 - A} = \frac{-50K}{\frac{1}{2}\left(1+\frac{1}{10}\right)^2 - 0.8} \approx 256K$$

This is the case of Lower Critical Solution Temperature, because χ increases with temperature increase. Thus the miscibility range is $T < T_C \sim 256K$.

3. Two polymers have lengths $N_1=100$ and $N_2=400$ and polymer-polymer interaction parameter $\chi=0.5K/T+0.01$. Estimate the temperature range of miscibility and critical volume composition.

$$T_C = \frac{B}{\frac{1}{2}\left(\frac{1}{\sqrt{N_1}} + \frac{1}{\sqrt{N_2}}\right)^2 - A} = \frac{0.5K}{\frac{1}{2}\left(\frac{1}{10} + \frac{1}{20}\right)^2 - 0.01} = 400K$$

This is an Upper Critical Solution Temperature because c decreases with temperature. Then the miscibility range $T > T_C = 400K$.

$$\phi_c = \frac{\sqrt{N_2}}{\sqrt{N_1} + \sqrt{N_2}} = \frac{2}{3}$$

Critical volume composition is $\phi_1=1/3$ and $\phi_2=2/3$.